

# Enhanced Line of Sight Velocity Analysis Using an Aperiodic Pulse Sequence on the Kodiak and King Salmon Radars.

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# The Ideal Multi-Pulse Sequence

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## **The goals to be achieved simultaneously include:**

- Provide long lags to increase low velocity resolution.
- Provide short lags to increase Nyquist upper bound.
- Maximize number of lags to increase available spectral information.

## **The constraints are:**

- Lags must not be repeated to minimize range aliasing.
- All lags must be a multiple of 10 usec for radar operation.

## **The resulting optimized multi-pulse sequence is:**

- A 16-pulse aperiodic pulse sequence designed by M. Balaji, and reported on last year.

# Why Use this Aperiodic Multi-Pulse Sequence?

Parameter	SuperDARN 8-pulse Sequence	Extended 16-pulse Sequence
Longest Lag Interval	36 ms	149.5 ms
Shortest Lag Interval	1.5 ms	0.4 ms
Number of Unique Lags	23	121
lags lost due to Tx-ON Rx-OFF conflicts 225 Range Gates, 15 km range resolution	30.4% 7	24% 29
Mean Nyquist Velocity at 12 MHz	3819 m/s	5013 m/s
Ability to resolve multiple components in a range cell	No	Yes

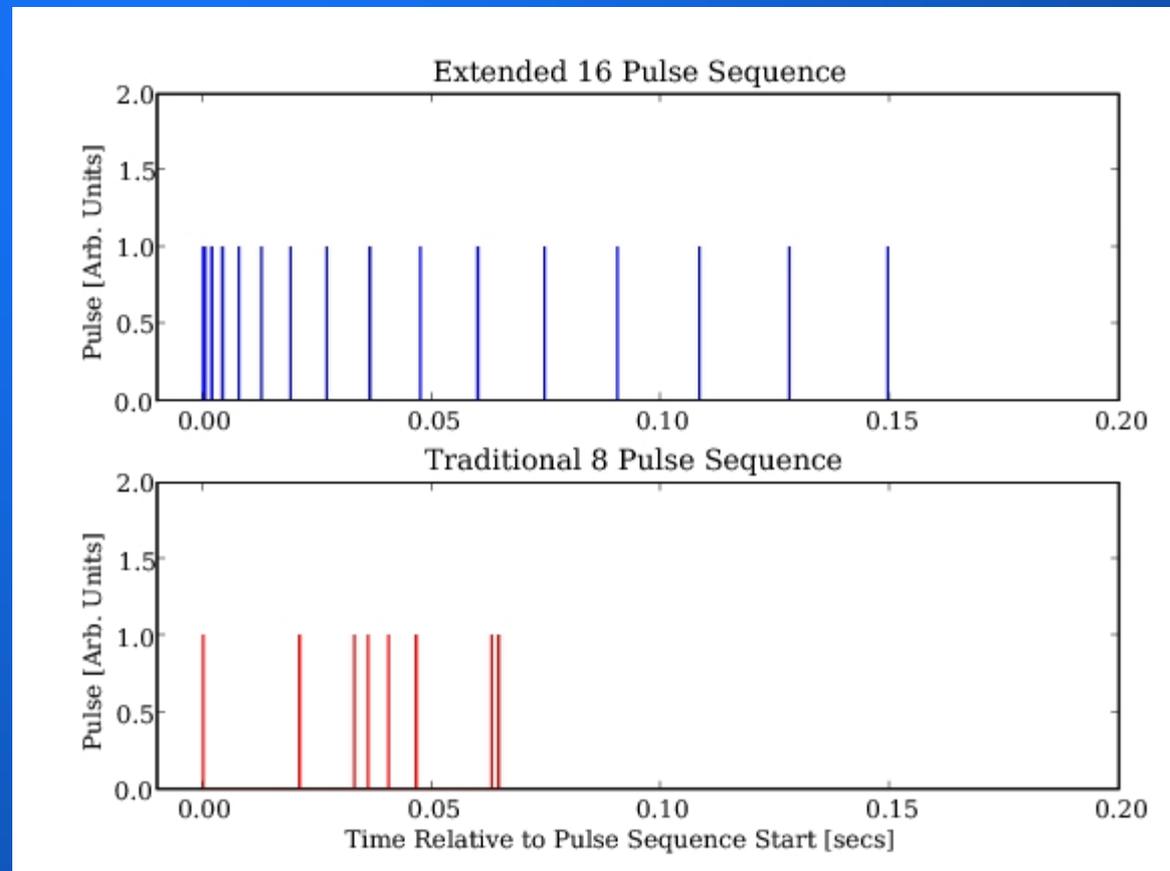
# Pulse Sequences Compared

## Extended Pulse Sequence:

- 16 pulses
- ~ 150 millisecond span

## Traditional Pulse Sequence:

- 8 pulses
- ~ 65 millisecond span

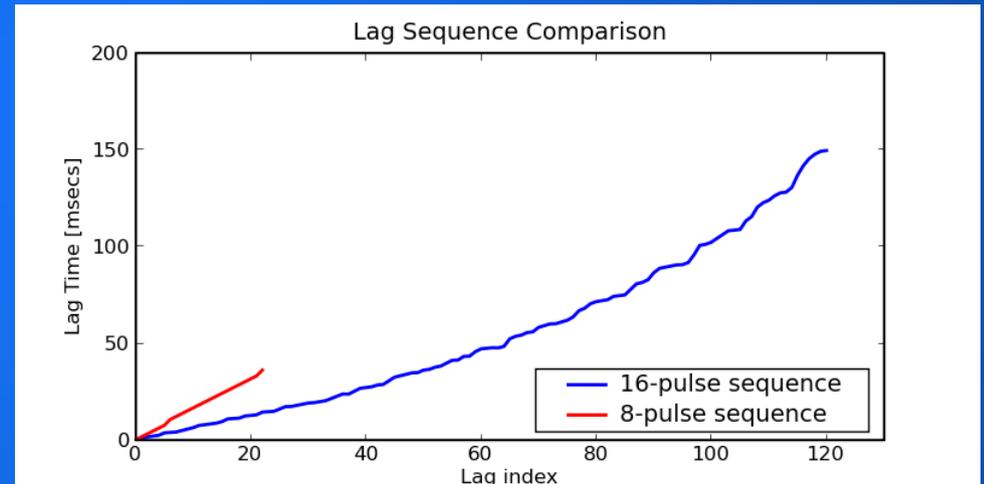


*(All pulses 100 microseconds long)*

# Lag Sequences Compared

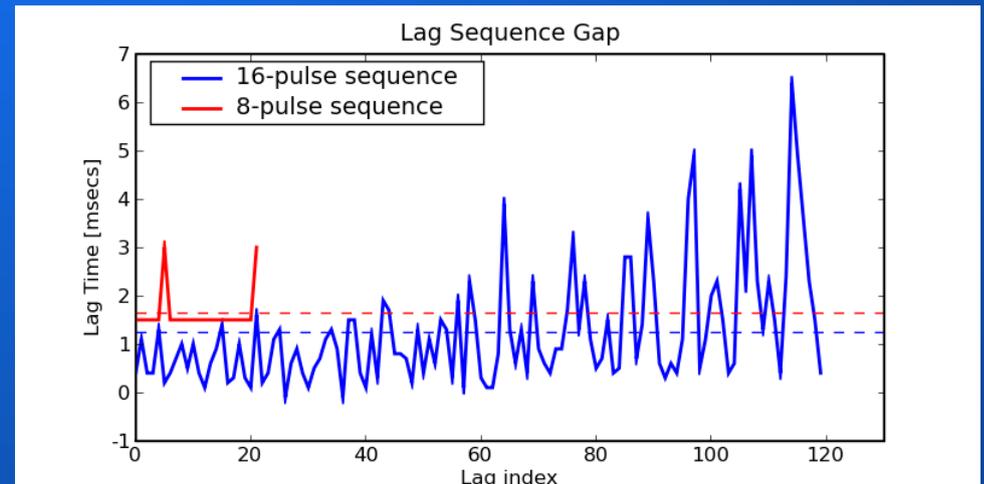
## Extended Lag Sequence:

- 121 lags
- ~ 150 millisecond span
- mpinc = 0.1 msec
- Many irregular lag intervals
- Average lag interval ~ 1.24 msec



## Traditional Lag Sequence:

- 23 lags
- ~ 36 millisecond span
- mpinc = 1.5 msec
- *Nearly* regular lag intervals
- Average lag interval ~ 1.63 msec

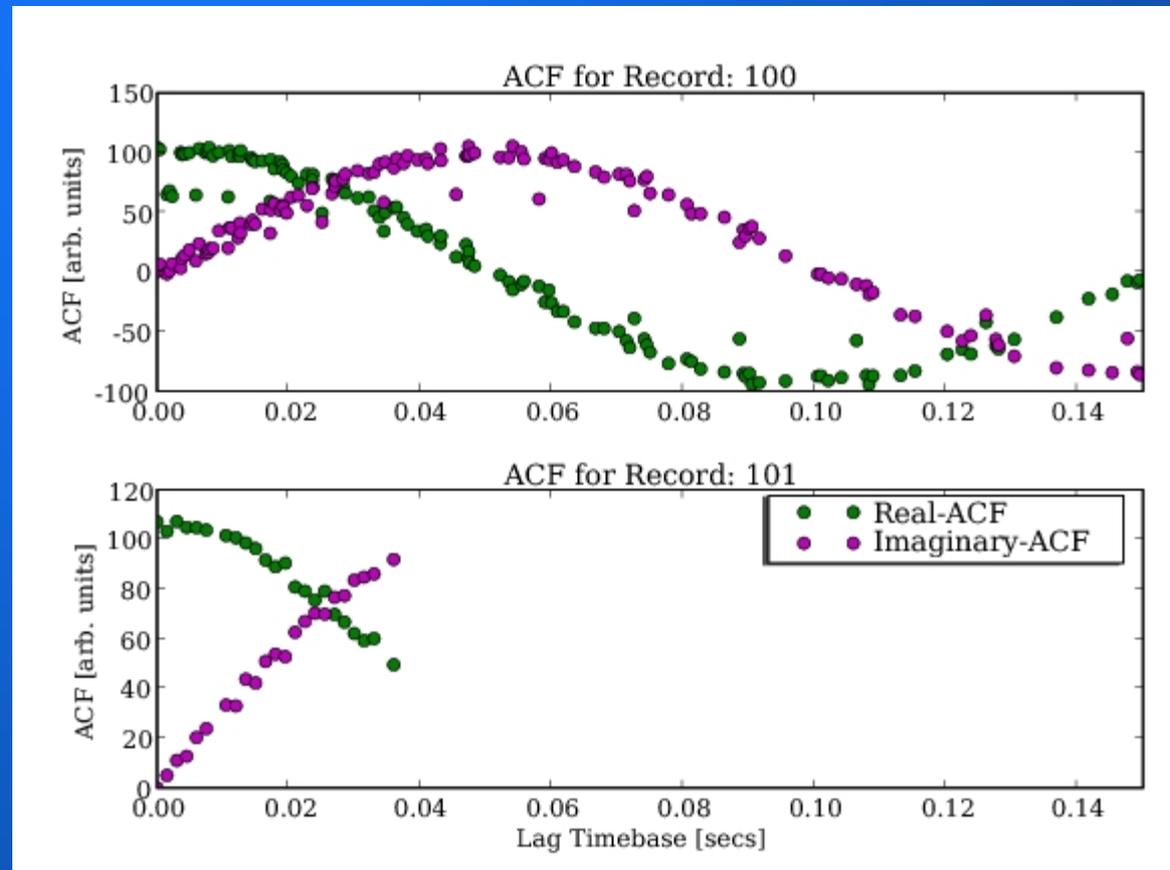


# ACF Comparison

Extended Pulse Sequence:  
6 second integration

Range: ~375 km

Traditional Lag Sequence:  
6 second integration



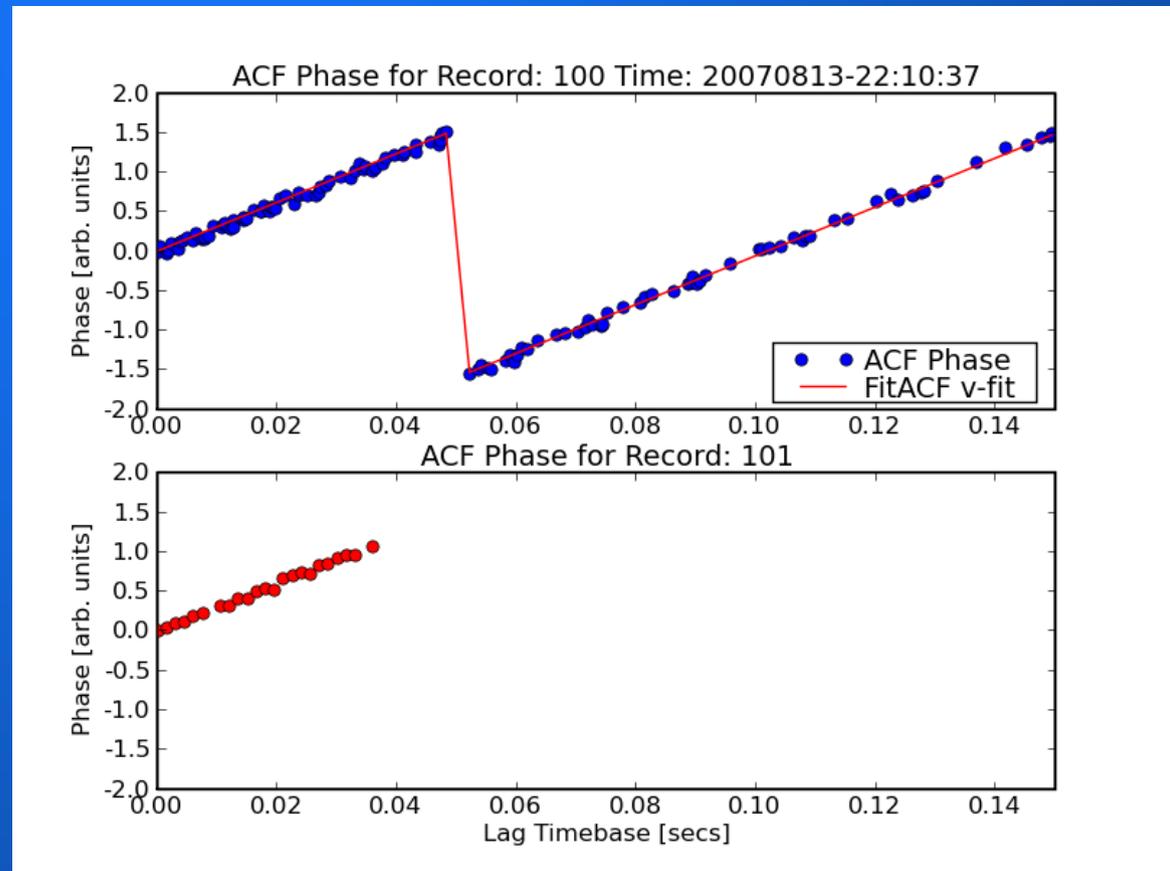
Experimental data from 2007-08-13 ~ 22:10 UTC

# Phase Comparison

Extended Lag Sequence:

Example of a target with  
FITACF  $v \sim 50$  m/s

Traditional Lag Sequence:



Experimental data from 2007-08-13 ~ 22:10 UTC

# Need to Enhance Velocity Fitting to Recover Spectral Information

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- ACFFIT Doppler frequency fitting uses a least squares fit of ACF phase:  $\Phi = \omega t$   
giving line of sight velocity as:  $v = c * (\omega) / (4 * \pi * f)$
- Assumes a single velocity target.
- Candidate techniques for estimating Doppler frequency spectrum include:
  - **Lomb Periodogram**
  - Maximum Entropy Spectral Estimation
  - SparSpec Algorithm

# An Introduction to the Lomb Periodogram

The Lomb periodogram uses sinusoidal model functions to fit the data of the form:

$$d(t_i) = A \cos(2\pi \omega t_i - \theta) - B \sin(2\pi \omega t_i - \theta) + n_i$$

The probability that the data is fitted by a model function for a given frequency is:

$$P_{LS}(\omega) = \frac{R_{LS}(\omega)^2}{C} + \frac{I_{LS}(\omega)^2}{S}$$

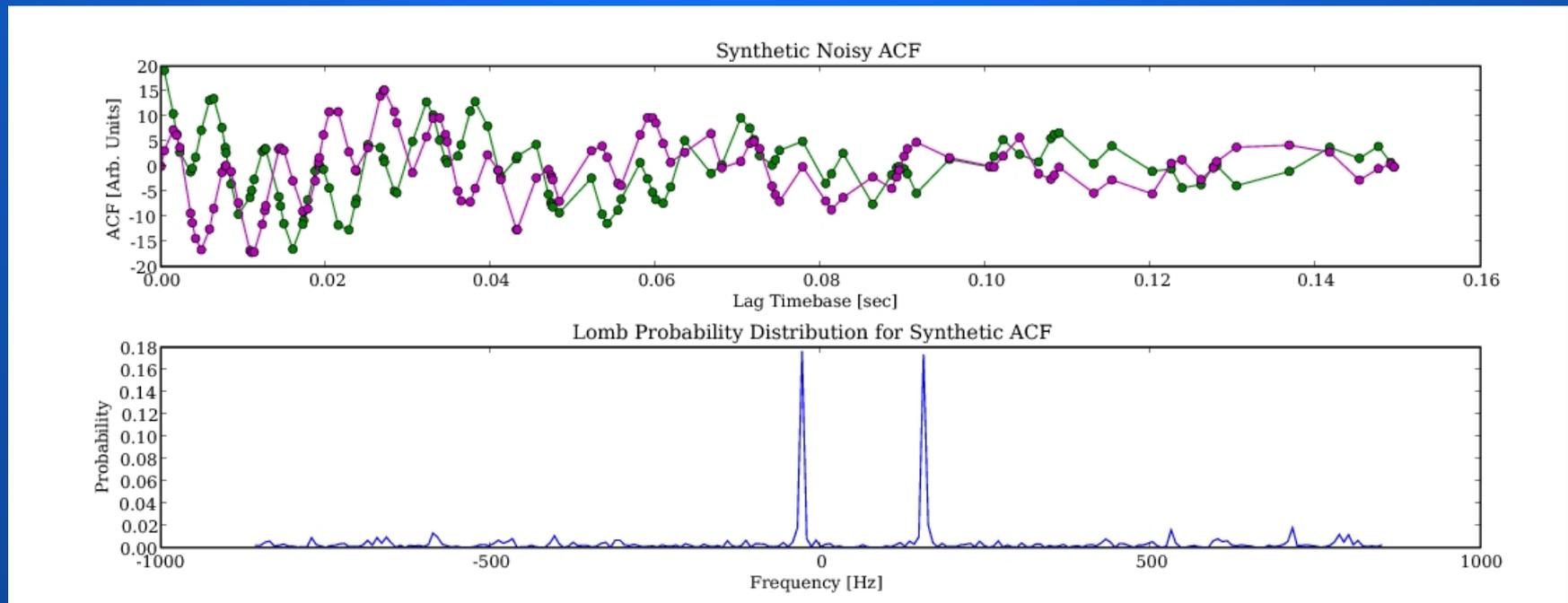
and using least squares constraints.

$$\begin{aligned} R_{LS} &\equiv \sum d(t_i) \cos(2\pi \omega t_i - \theta) & I_{LS} &\equiv \sum d(t_i) \sin(2\pi \omega t_i - \theta) \\ C &\equiv \sum \cos^2(2\pi \omega t_i - \theta) & S &\equiv \sum \sin^2(2\pi \omega t_i - \theta) \end{aligned}$$

$\theta$  is chosen so that the sine and cosine model functions are orthogonal on the aperiodic dataset  $d(t)$ .

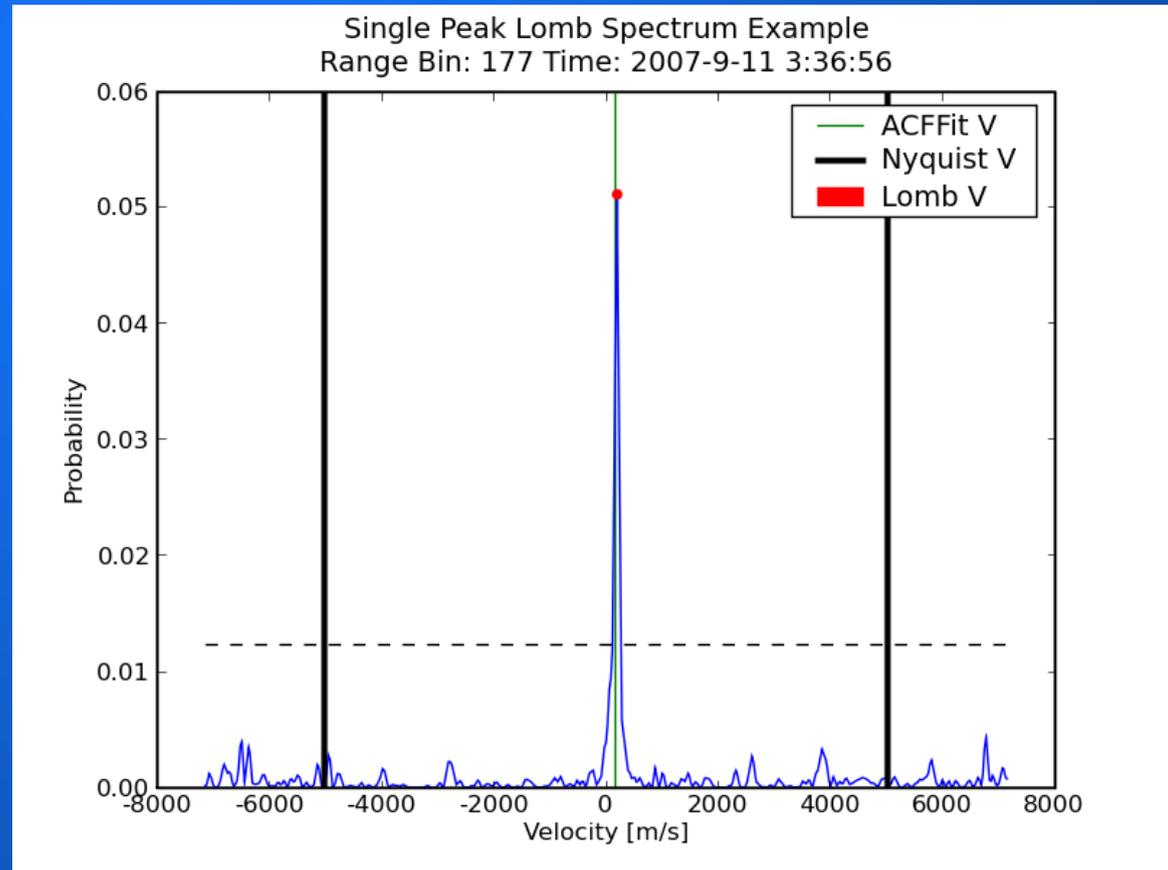
# Synthetic Example of Lomb Periodogram

- Synthetic noisy ACF constructed using -28 Hz and +156 Hz components.
- ACF sampled using the extended pulse sequence (16 pulses, 121 lags).

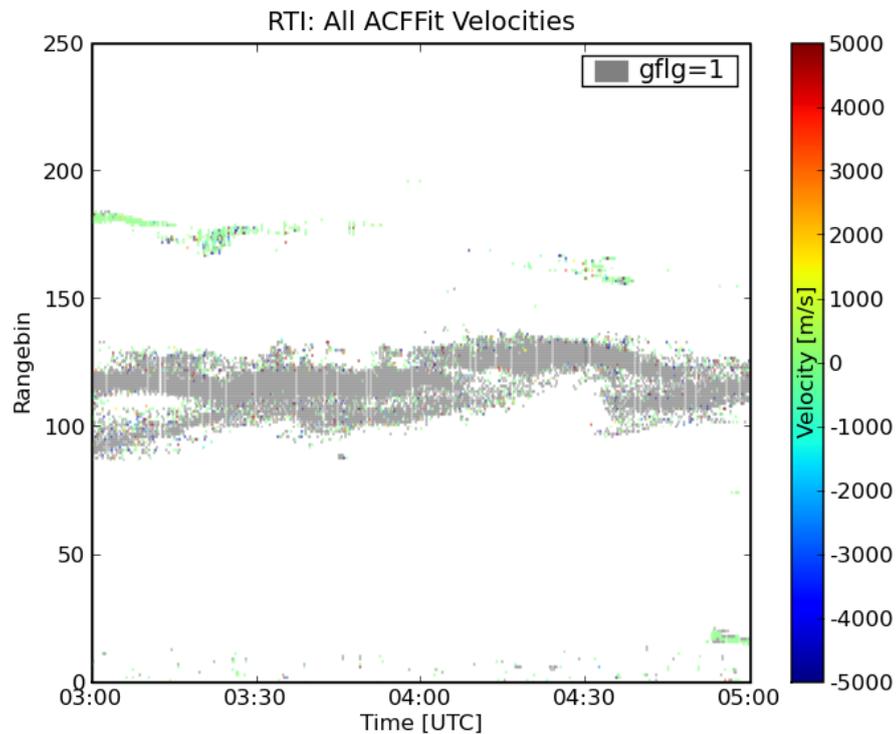


# Lomb Periodogram Example Using Kodiak Radar Data

- Peak Lomb velocity:  $\sim 200$  m/s
- Good agreement with ACFFIT Velocity  $\sim 160$  m/s
- Nyquist velocity:  $\sim 5000$  m/s



# Pulse Sequence Operational Comparison Along Beam 5

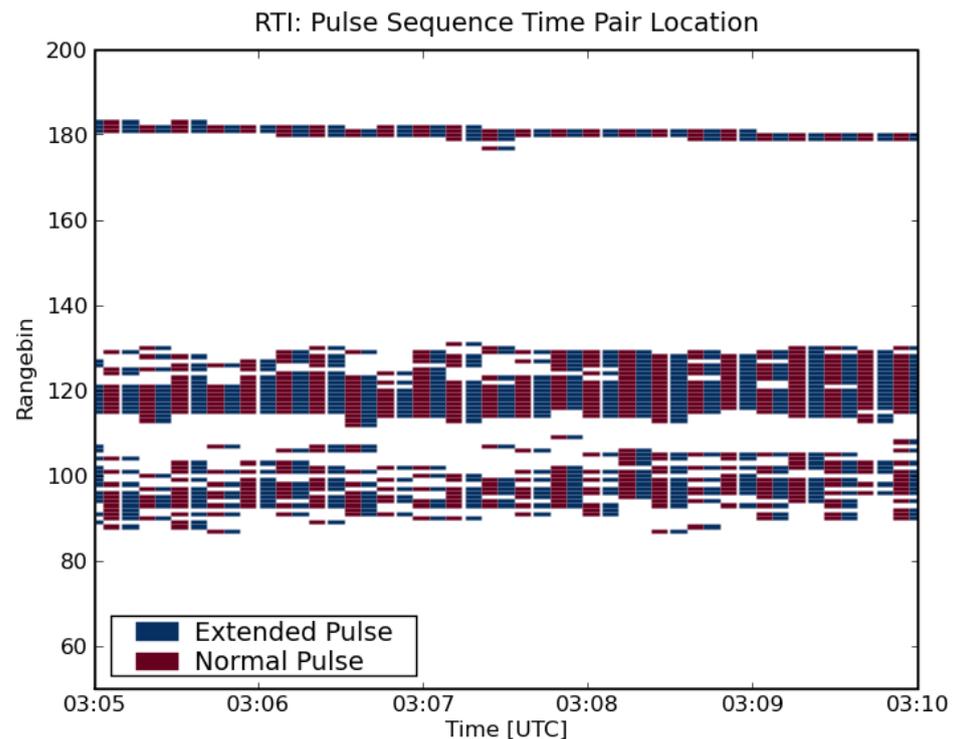
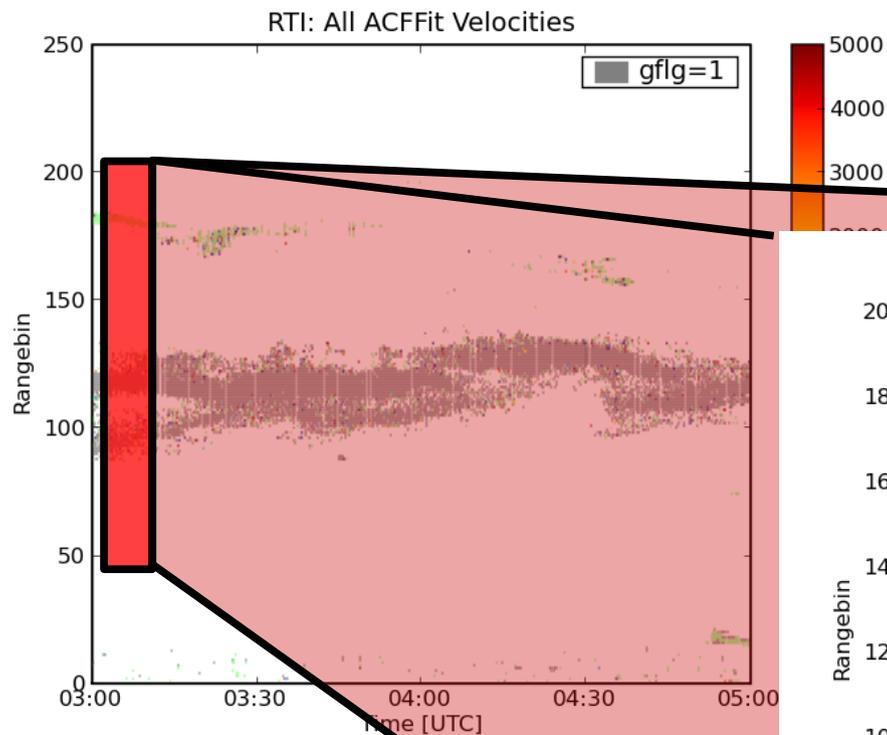


- Extended 16-pulse sequences interlaced with normal 8-pulse sequences
- ACF integration time : 6 seconds
- Beam Direction: 5

**Radar ACF data from Kodiak radar on 2007-09-11.**

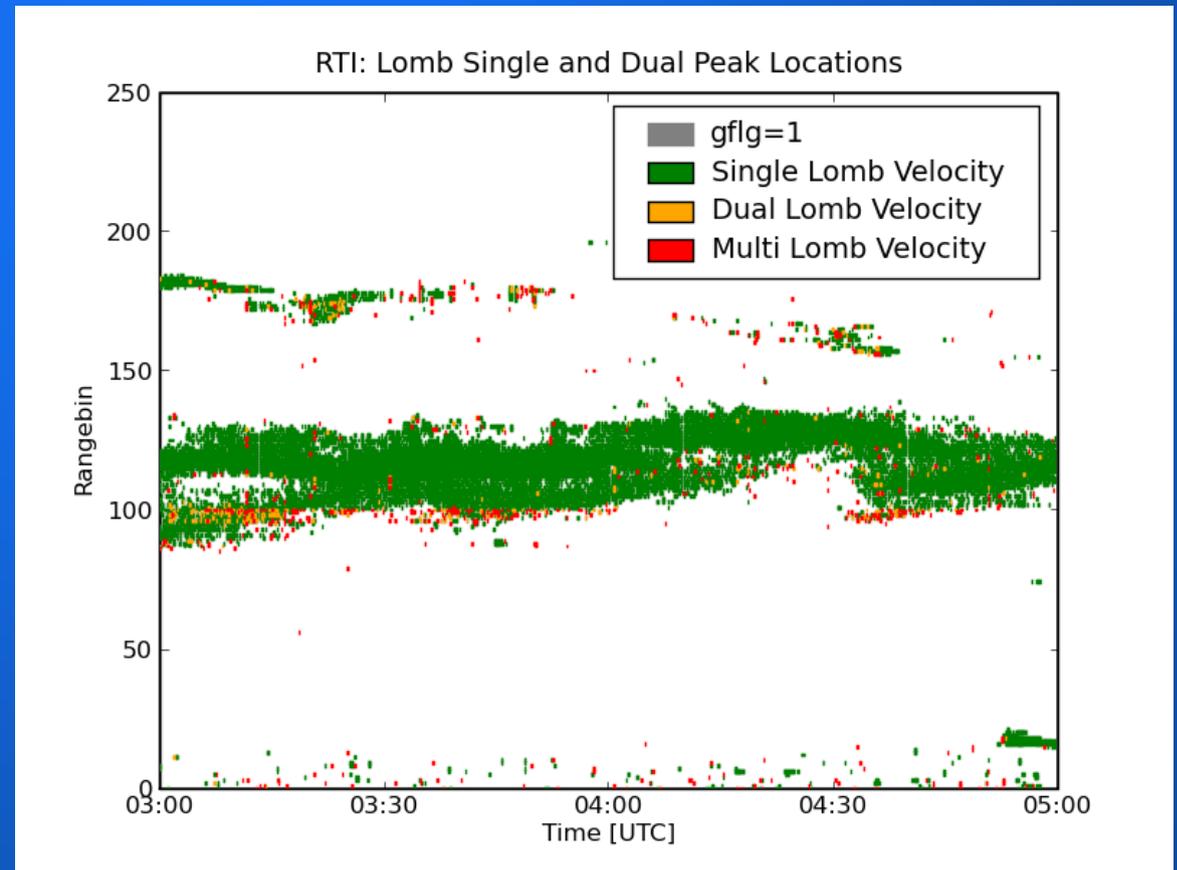
# Interlaced 16 and 8 Pulse Sequences for Time Paired Comparison

Analysis of only ranges with time-paired ACFFIT velocities.

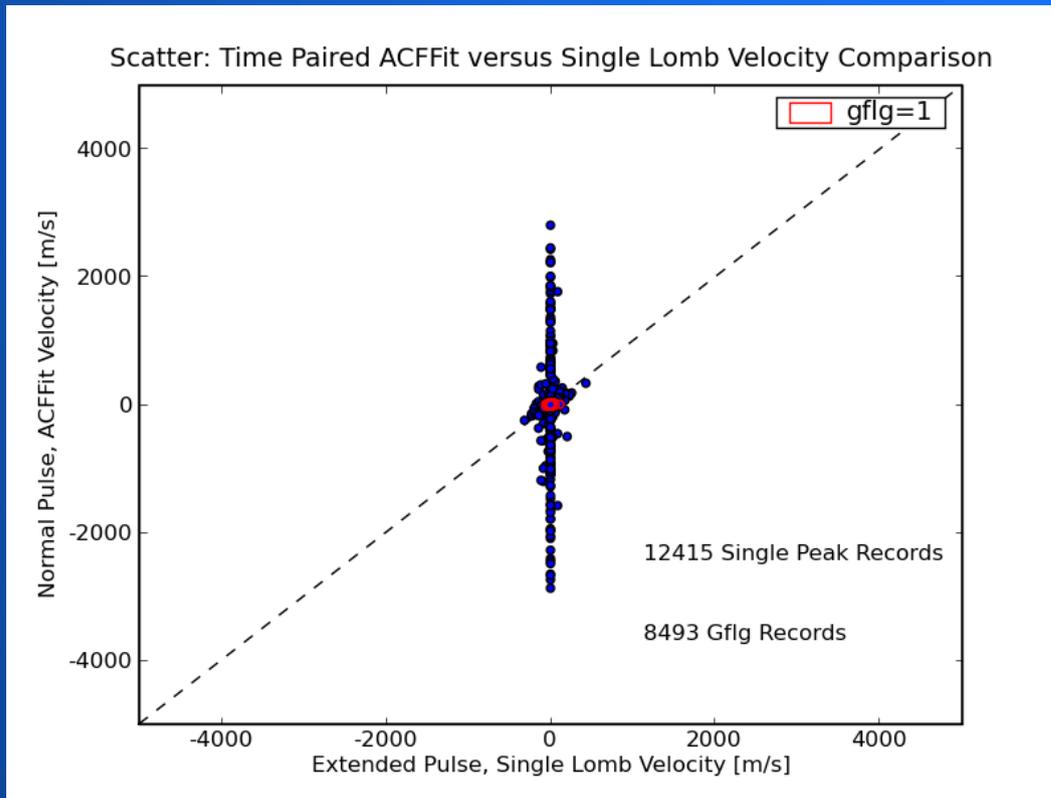


# Single Peak Lomb Velocity Analysis Dominates

- Single Lomb Records: 12415
- Dual Lomb Records: 329

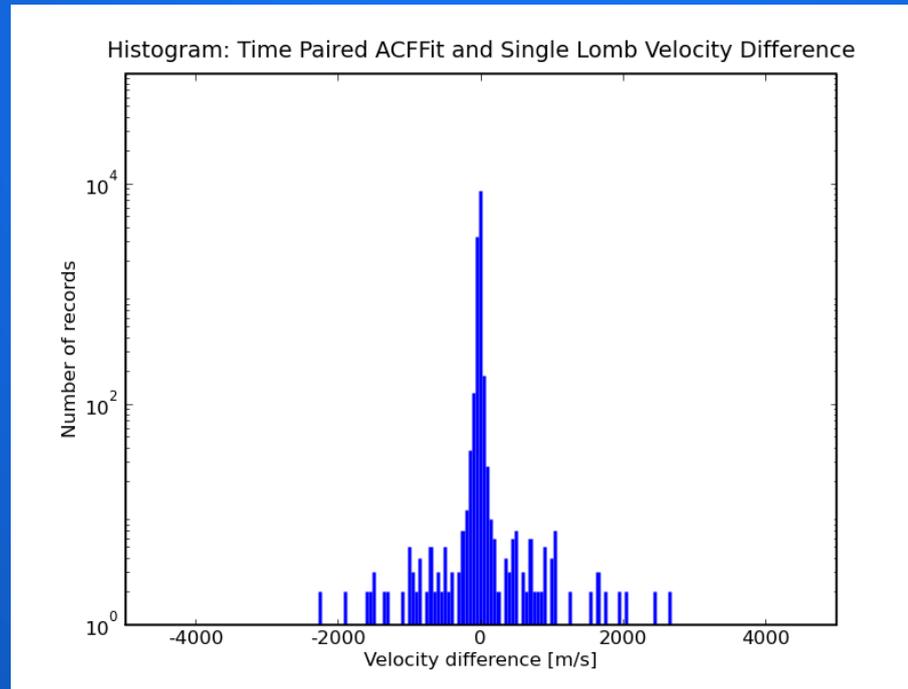


# Records with a Single Lomb Velocity Peak

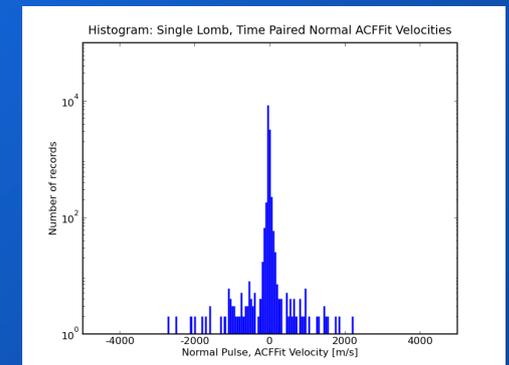


- 12415 time-paired records
- 8493 identified as groundscatter by ACFFit
- All Lomb velocities  $< 1000$  m/s

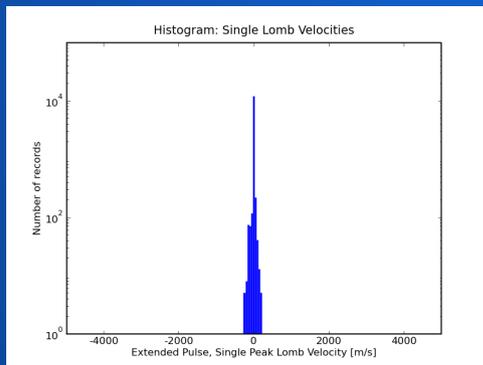
# Lomb Velocity Peak is Highly Correlated with ACFFIT Velocity



Most ACFFit and Lomb velocities agree within 50 m/s



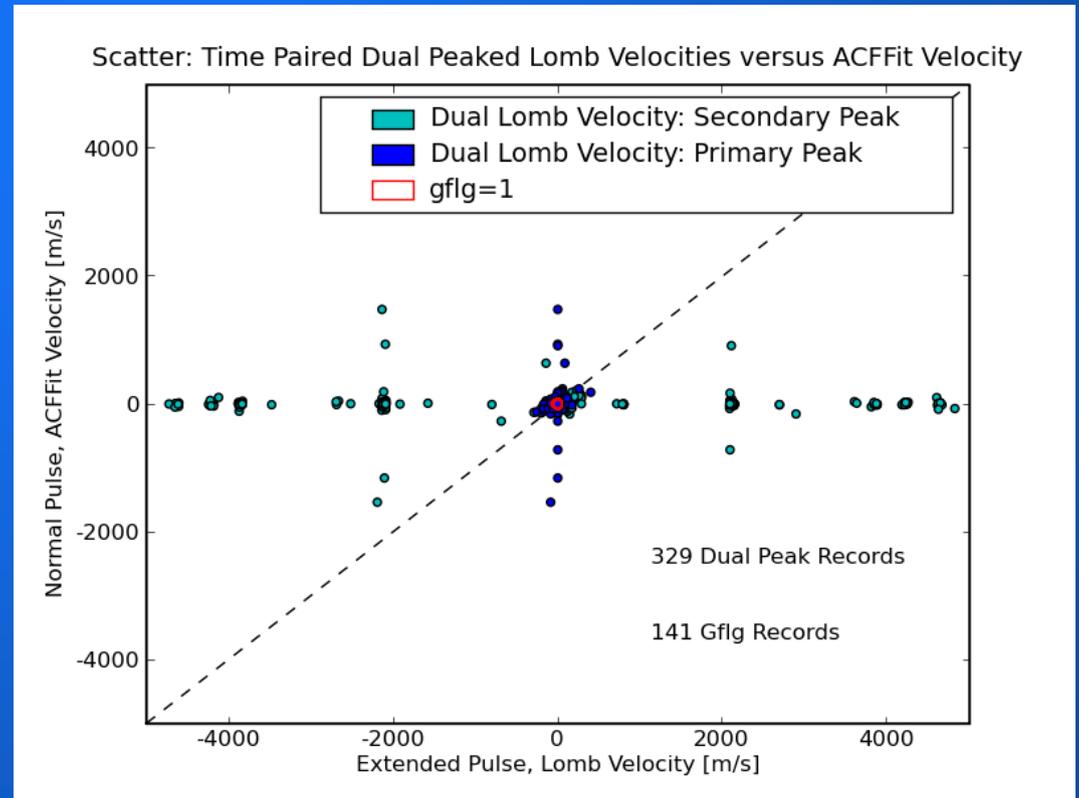
Normal pulse  
ACFFit velocity



Extended pulse  
Lomb peak velocity

# Records with Dual Lomb Velocity Peaks

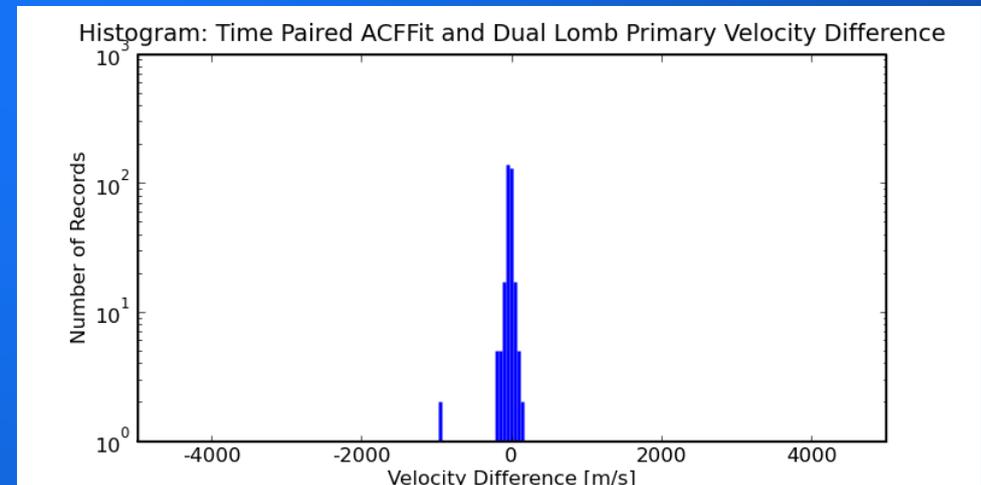
- 329 dual peak records
- 141 identified as groundscatter
- Most probable velocity is typically  $< 1000$  m/s
- Secondary Lomb velocity peaks cluster at velocities  $> 1000$  m/s



# Primary Velocity in Dual Peak Lomb Matches ACFFIT Velocity

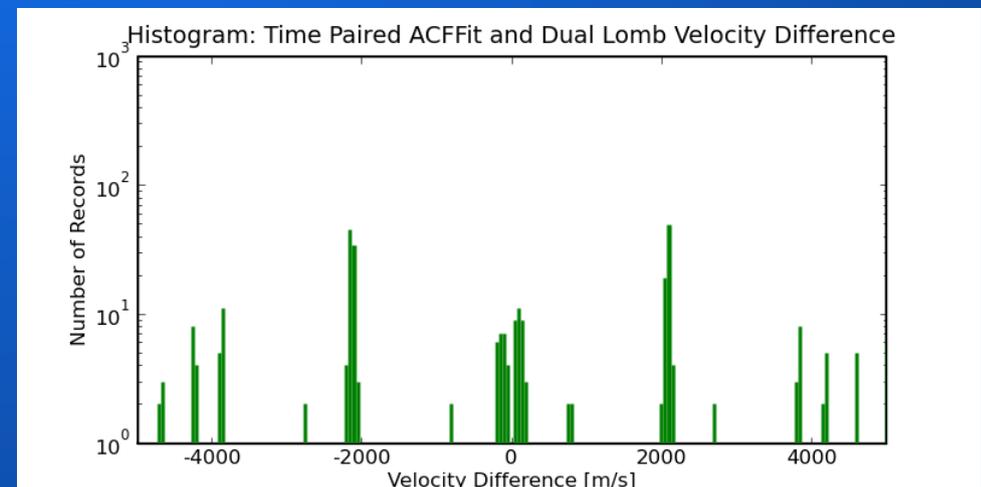
## Primary Lomb Velocity:

- Represents most probable velocity in Lomb analysis.
- Velocities are centered near 0 m/s and correlate well with ACFFit velocities.



## Secondary Lomb Velocity:

- Highly symmetric clustering of velocities away from 0 m/s.
- Clusters at 2000 m/s associated with records marked as groundscatter by ACFFit.



# Summary of Analysis

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- Analysis was conducted for a relatively quiet ionosphere, with radar data dominated by groundscatter returns.
- Time-paired extended pulse Lomb and normal ACFFit analysis agree as to the single component nature of the majority of the available line of sight velocity data.
- ~ 3% of the observed pulse ranges have dual Lomb velocity peaks. Multiple peaked ranges have yet to be taken into account.
- Of the dual peak records, the secondary peak velocity distribution also showed an unexplained symmetric behavior not accounted for by sample aliasing.

# Future Work

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- Implement new peak detection algorithm for use with Lomb analysis.
- Finish implementing complex valued SparSpec algorithm and compare with Lomb velocity analysis results for existing data set.
- Acquire extended pulse data during active ionospheric backscatter activity.